

1. Convert the polar coordinates $(-2, \frac{\pi}{3})$ to rectangular coordinates.
- A. $(1, -\sqrt{3})$ C. $(-1, \sqrt{3})$ E. NOTA
 B. $(-1, -\sqrt{3})$ D. $(1, \sqrt{3})$
2. Identify the graph with equation: $x^2 - 2xy + y^2 = 4$.
- A. Ellipse C. 2 Parallel Lines E. NOTA
 B. Circle D. 2 Intersecting Lines
3. Find a possible equation for the following ellipse:
- A. $\frac{(x+1)^2}{9} + \frac{(y-2)^2}{4} = 1$
 B. $\frac{(x-1)^2}{9} + \frac{(y+2)^2}{4} = 1$
 C. $\frac{(x+1)^2}{36} + \frac{(y-2)^2}{64} = 1$
 D. $\frac{(x-1)^2}{36} + \frac{(y+2)^2}{64} = 1$
 E. NOTA

4. Find the eccentricity for the graph in Question 3.

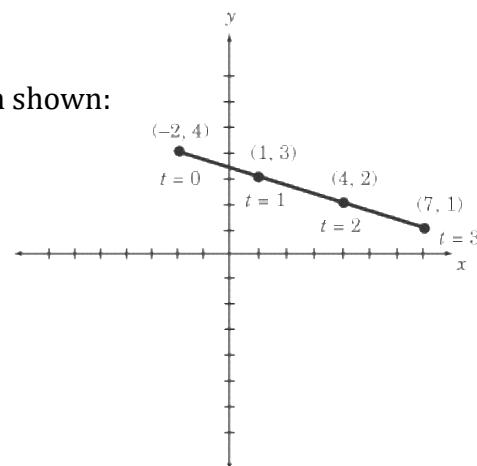
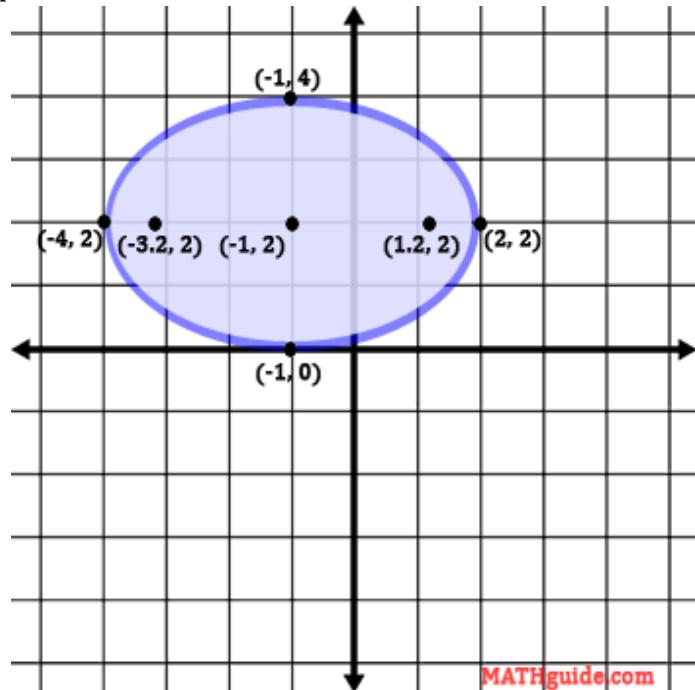
- A. $\frac{\sqrt{5}}{2}$
 B. $\frac{\sqrt{13}}{2}$
 C. $\frac{3}{2}$
 D. $\frac{2\sqrt{5}}{5}$
 E. NOTA

5. Find the area contained within the graph in Question 3.

- A. 18π C. 6π E. NOTA
 B. 12π D. 2π

6. Find a set of parametric equations for the graph shown:

- A. $x = -2 - 3t$ $y = 4 + t$ $t | 0 \leq t \leq 3$
 B. $x = 3 - 2t$ $y = -1 + 4t$ $t | 0 \leq t \leq 3$
 C. $x = -2 + 3t$ $y = 4 - t$ $t | 0 \leq t \leq 3$
 D. $x = -2 + 3t$ $y = 4 - t$ $t | 0 < t < 3$
 E. NOTA



7. Using the given projectile motion equations, find the maximum height in meters of a baseball tossed at an initial angle of 60 degrees and speed of 5 meters per second. Assume the ball is traveling as a projectile and that gravity is 10 meters per square second.

$$\begin{aligned}\text{Time of flight} &= \frac{2v_0 \sin \theta}{g} \\ \text{Maximum height reached} &= \frac{v_0^2 \sin^2 \theta}{2g} \\ \text{Horizontal range} &= \frac{v_0^2 \sin 2\theta}{g}\end{aligned}$$

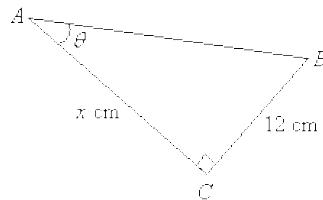
- A. $\frac{5}{48}$
 B. $\frac{15}{16}$
 C. $\frac{5\sqrt{3}}{4}$
 D. $\frac{15\sqrt{3}}{16}$
 E. NOTA

8. Find the horizontal range of the baseball from Question 7:

- A. $\frac{5}{48}$
 B. $\frac{15}{16}$
 C. $\frac{5\sqrt{3}}{4}$
 D. $\frac{15\sqrt{3}}{16}$
 E. NOTA

9. What is the value of x if $\theta = \frac{\pi}{3}$ in Triangle ABC?

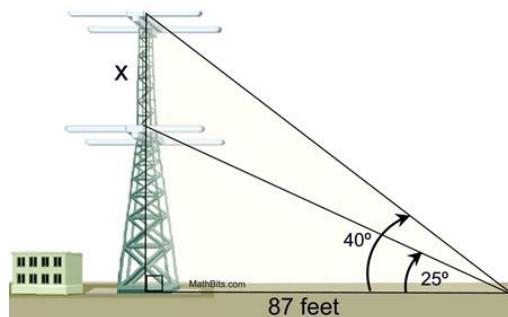
- A. $2\sqrt{3}$
 B. $4\sqrt{3}$
 C. 6
 D. 9
 E. NOTA



10. Solve for x in feet on the tower diagram. Use the approximations:

$$\tan 40^\circ \approx 0.84 \text{ and } \tan 25^\circ \approx 0.47$$

- A. 54.12
 B. 45.67
 C. 34.87
 D. 32.19
 E. NOTA



11. Find the height of the tower from Question 10.

- A. 67.91
 B. 73.08
 C. 92.34
 D. 100.45
 E. NOTA

12. Simplify: $\frac{\cot(x) \sin(x)}{\cos(x)}$

- A. $\cos^2 x$
 B. $\sin^2 x$
 C. $\cot^2 x$
 D. $\sin^3 x$
 E. NOTA

13. Find the area of the polar graph of $r = 4\sin\theta$

- A. 12π
 B. 8π
 C. 4π
 D. 2π
 E. NOTA

14. Find the center of the graph in polar coordinates for Question 13.

- | | | |
|---------------------------|--------------------------|---------|
| A. $(-4, -\frac{\pi}{2})$ | C. $(-2, \frac{\pi}{2})$ | E. NOTA |
| B. $(2, -\frac{\pi}{2})$ | D. $(2, \frac{\pi}{2})$ | |

15. Find the circumference of the graph for Question 13.

- | | | |
|------------|-----------|---------|
| A. 12π | C. 4π | E. NOTA |
| B. 8π | D. 2π | |

16. Solve $\tan\left(\frac{\theta}{2}\right) = \sqrt{3}$ on the interval $0 < \theta < 4\pi$. Find the sum of all values of θ .

- | | |
|----------------------|-----------|
| A. $\frac{11\pi}{3}$ | C. 3π |
| B. $\frac{10\pi}{3}$ | D. 2π |
| | E. NOTA |

17. Solve for x on $[-2\pi, 0)$ for $2\sin^2 x - 3\sin x = 2$.

- | | | |
|--|--|---------|
| A. $x = -\frac{5\pi}{6}, -\frac{11\pi}{6}$ | C. $x = -\frac{5\pi}{6}, -\frac{7\pi}{6}$ | E. NOTA |
| B. $x = -\frac{7\pi}{6}, -\frac{11\pi}{6}$ | D. $x = -\frac{5\pi}{6}, -\frac{13\pi}{6}$ | |

18. Solve: $\begin{vmatrix} -3 & 0 & 1 \\ -2 & 10 & 4 \\ 6 & -1 & 0 \end{vmatrix}$.

- | | | |
|--------|--------|---------|
| A. -50 | C. -70 | E. NOTA |
| B. -60 | D. -80 | |

19. Solve: $\begin{vmatrix} e^0 & \frac{0}{4} & \tan 0 \\ \sqrt[3]{-8} & \sec \pi & \log_2 128 \\ 3! & \cot \frac{\pi}{2} & \left(\frac{1}{2}\right)^{-3} \end{vmatrix}$.

- | | | |
|-------|--------|---------|
| A. -1 | C. -8 | E. NOTA |
| B. -4 | D. -16 | |

20. Simplify to solve the equation: $4\log_9 x + 8 = 12$

- | | | |
|-------------|------------|---------|
| A. $x = 9$ | C. $x = 3$ | E. NOTA |
| B. $x = 81$ | D. $x = 4$ | |

21. Out of forty-five students, 14 are taking English and 29 are taking Physics. 8 students are taking both. What is the probability that a randomly-chosen student from this group is taking only the Physics class?

- | | | |
|-------------------|--------------------|---------|
| A. $\frac{2}{15}$ | C. $\frac{7}{15}$ | E. NOTA |
| B. $\frac{4}{15}$ | D. $\frac{11}{15}$ | |

22. Find $P(\text{student taking English}|\text{student taking Physics})$ for Question 21.

- | | | |
|-------------------|-------------------|---------|
| A. $\frac{8}{45}$ | C. $\frac{2}{15}$ | E. NOTA |
| B. $\frac{8}{29}$ | D. $\frac{8}{15}$ | |

23. MU University wants to make student ID badges with a code consisting of 2 different letters followed by 4 different digits. How many possible ID codes could the university have?

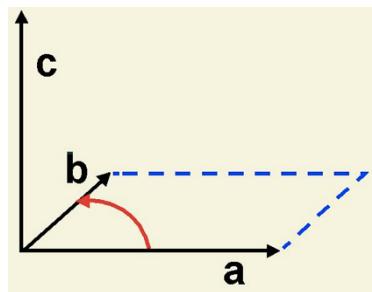
- | | | |
|----------------------------|-------------------------------|---------|
| A. $(7)(8)(9)(10)(25)(26)$ | C. $(10)(10)(10)(10)(25)(26)$ | E. NOTA |
| B. $(7)(8)(9)(10)(26)(26)$ | D. $(26)(26)(10)(10)(10)(10)$ | |

24. What is the probability that an ID code from Question 23 would have two traditional vowels?

- | | | |
|--------------------|-------------------|---------|
| A. $\frac{10}{13}$ | C. $\frac{1}{26}$ | E. NOTA |
| B. $\frac{9}{65}$ | D. $\frac{2}{65}$ | |

25. Vector c is perpendicular to the two given vectors a and b . What expression could equal c ?

- | | |
|-----------------|------------|
| A. $a \cdot b$ | D. $a + b$ |
| B. $a \times b$ | E. NOTA |
| C. ab | |



26. Find the absolute value of the triple scalar product of the vectors: $\langle 2,3,4 \rangle$,

$$\langle -1,1,-1 \rangle \quad \text{and} \quad \langle -1,-3,-5 \rangle.$$

- | | | |
|------|------|---------|
| A. 1 | C. 3 | E. NOTA |
| B. 2 | D. 4 | |

27. Find the equation of the directrix of the graph of the equation in polar: $r = \frac{12}{4-4\cos\theta}$.

- | | | |
|-----------------------|-----------------------|---------|
| A. $r = -3\sec\theta$ | C. $r = -3\csc\theta$ | E. NOTA |
| B. $r = 3\sec\theta$ | D. $r = 3\csc\theta$ | |

28. Given the function: $f(x) = \begin{cases} x-2 & x < -3 \\ x^2 & x \geq -3 \end{cases}$, find $\lim_{x \rightarrow -3^+} f(x)$.

- | | | |
|-------|-------------------|---------|
| A. 1 | C. 9 | E. NOTA |
| B. -5 | D. Does Not Exist | |

29. An angle of $\frac{5\pi}{12}$ lies at the center of a circle and subtends an arc of the circle. If the diameter of the circle is 8 units, find the arc length.

- | | | |
|----------------------|---------------------|---------|
| A. $\frac{10\pi}{3}$ | C. $\frac{2\pi}{3}$ | E. NOTA |
| B. $\frac{5\pi}{3}$ | D. $\frac{\pi}{3}$ | |

30. Give the number of distinct permutations of the letters in the word BASEBALL.

- | | |
|-------------------------|--|
| A. 2520 | |
| B. 5040 | |
| C. 10080 | |
| D. Cannot be determined | |
| E. NOTA | |